

DO NOW

What methods have we learned to solve a quadratic equation?

1. Set = 0 ; factor
2. Completing the square
3. graph \rightarrow x-intercepts
4. table \rightarrow y=0

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8.8 The Quadratic Formula

*** used to solve unfactorable quadratic equations

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Procedure:

1. Write the equation in standard form.
2. Identify $a =$, $b =$, and $c =$.
3. Write the quadratic formula.
4. Substitute
5. Simplify

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Answers from the quadratic formula:

\rightarrow exact answers will usually contain a radical.

* Only give decimal answers if asked to approximate.

Examples:

$$\begin{aligned} 1. \quad 4x^2 - 12 &= 5x \\ 4x^2 - 5x - 12 &= 0 \\ a &= 4 \\ b &= -5 \\ c &= -12 \\ x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\ x &= \frac{-(-5) \pm \sqrt{(-5)^2 - 4(4)(-12)}}{2(4)} \end{aligned}$$

$$\begin{aligned} x &= \frac{5 \pm \sqrt{25 - 16(-12)}}{8} \\ x &= \frac{5 \pm \sqrt{25 + 192}}{8} \\ x &= \boxed{\frac{5 \pm \sqrt{217}}{8}} \end{aligned}$$

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$$2. \quad 2x^2 + 4x = 14$$

$$2x^2 + 4x - 14 = 0$$

$$a = 2$$

$$b = 4$$

$$c = -14$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-4 \pm \sqrt{4^2 - 4(2)(-14)}}{2(2)}$$

$$x = \frac{-4 \pm \sqrt{16 - 8(-14)}}{4}$$

$$x = \frac{-4 \pm \sqrt{16 + 112}}{4}$$

$$x = \frac{-4 \pm \sqrt{128}}{4}$$

$$x = \frac{-4 \pm \sqrt{64}}{4}$$

$$x = \frac{-4 \pm 8\sqrt{2}}{4}$$

$$x = \frac{-4}{4} \pm \frac{8\sqrt{2}}{4}$$

$$x = -1 \pm 2\sqrt{2}$$

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$$3. \quad 3x^2 - 4x = 14$$

$$\begin{aligned} 3x^2 - 4x - 14 &= 0 \\ a &= 3 \\ b &= -4 \\ c &= -14 \\ x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\ x &= \frac{4 \pm \sqrt{(-4)^2 - 4(3)(-14)}}{2(3)} \\ x &= \frac{4 \pm \sqrt{16 - 12(-14)}}{6} \\ x &= \frac{4 \pm \sqrt{16 + 168}}{6} \\ x &= \frac{4 \pm \sqrt{184}}{6} \end{aligned}$$

$$\begin{aligned} x &= \frac{4 \pm \sqrt{4 \cdot 46}}{6} \\ x &= \frac{4 \pm 2\sqrt{46}}{6} \\ x &= \frac{4}{6} \pm \frac{2\sqrt{46}}{6} \\ x &= \frac{2}{3} \pm \frac{\sqrt{46}}{3} \\ x &= \boxed{\frac{2 \pm \sqrt{46}}{3}} \end{aligned}$$

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HOMEWORK

Worksheet - HW 8.8
The Quadratic Formula

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